

## Introduction

- ▶ **Goal**
  - Investigate efficient parallel strategies under heterogeneous computing systems.
  - Our **research** interests are of **Linear Solvers** especially for **Krylov Subspace Methods** and their **BLAS**. (axpy, dot, and spmv)
- ▶ **Strategies**
  - Data parallel: Load Balancing
  - Task parallel: Supplementary Acceleration

## Target Platforms

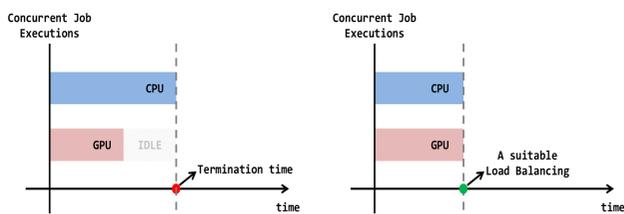
- ▶ **HAECHI (4 nodes)**
  - High-performance Applications for Extreme-scale Computing with Heterogeneous Infrastructure.
    - 2 CPUs (Xeon E5-2650) and 3 GPUs (HD 7950)
    - Optional: Xeon Phi (7120P), FPGA (Nallatech 395)
- ▶ **Target Devices**
  - One CPU and GPU
  - Node level parallelism

## Target Applications

- ▶ **Basic Linear Algebraic Subroutines (BLAS)**
  - Core algorithms for linear solvers
  - axpy, dot, norm2, spmv
- ▶ **Krylov Subspace Methods ( $Ax = b$ )**
  - Preconditioned approaches are considered
    - To guarantee robustness for general system
    - Include preconditioned CG and BiCG
    - Approximated inverse preconditioning

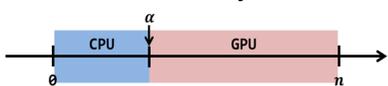
## Data Parallel Strategy

### Motivation



### Load Balancing

- ▶ Assume we have  $n$  numbers of data parallelizable jobs.
- ▶ We propose a job splitting ratio called  $\alpha$  which divides workloads into  $\alpha n$  and  $(1 - \alpha)n$  jobs so that assign  $\alpha n$  jobs into the CPU and  $(1 - \alpha)n$  jobs for the GPU.



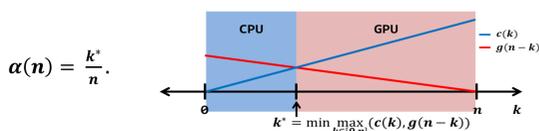
### min-max Model for $\alpha$

For given  $n$ , find a splitting point  $k^*$  which is the solution of the following min-max problem.

$$J(k^*; n) = \min_{k \in [0, n]} J(k; n)$$

where  $J(k; n) = \max(c(k), g(n - k))$

$c(k)$  denotes elapsed time for input  $k$  using CPU and  $g(n - k)$  denotes elapsed time for input  $n - k$  using GPU. The splitting ratio  $\alpha$  with given  $n$  is defined as follows.

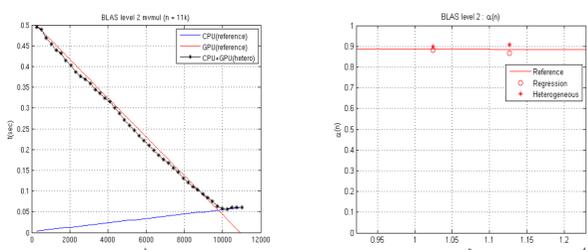


### Result (BLAS sgemv)

ENV: AMD OpenCL SDK 2.8, CPU: AMD FX 8120, GPU: HD7950

$$c(n) = \frac{4 \text{bytes} \times (n + 2)}{B_{CPU}} n + \frac{n^2}{F_{CPU}} + O_{CPU}$$

$$g(n) = \frac{4 \text{bytes} \times (n + 1)}{B_{PCI,W}} n + \frac{4 \text{bytes}}{B_{PCI,R}} n + \frac{4 \text{bytes} \times (n + 2)}{B_{GPU}} n + \frac{n^2}{F_{GPU}} + O_{GPU}$$



values	Heterogeneous	Regression	Reference
Splitting ratio ( $\alpha$ )	0.909	0.868	0.881
Execution time	0.05624 sec	0.06078 sec	0.06078 sec
Differences		0.00454 sec	0.00454 sec

## Task Parallel Strategy

### Motivation

- ▶ Iterative Krylov subspace methods (KSM) are composed of several routines of BLAS.
- ▶ **Data-parallel strategy** is seemed to be an easy approach, but has **poor load balancing** about **9:1 (CPU:GPU)** which was caused by performance gaps of memory bandwidth.

### Preconditioned KSM

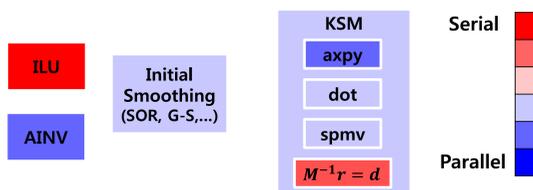
- ▶ KSMs cover specific scopes of their usages with respect to characteristics of linear system.
- ▶ Preconditioning methods are better choices when it comes to consider about robustness of linear solvers.
- ▶ Of course, one should pay additional costs for preconditioning which may not fit well parallel implementation.

### Well-known Two Preconditioners

$$Ax = b \quad MAx = Mb$$

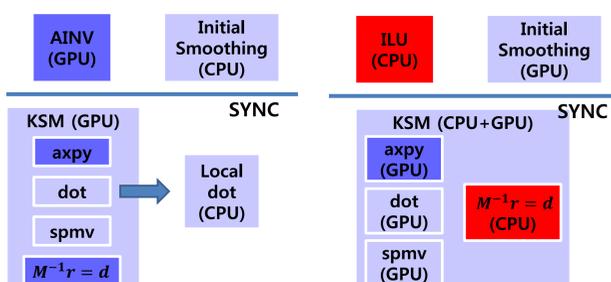
- ▶ A good preconditioner is to choose  $M$  to be closed to  $A^{-1}$ .
- ▶ The heaviest cost is solving additional system  $M^{-1}r = d$ .
- ▶ **Incomplete Factorization** (IC, ILU, ILUT, ...)
- ▶ **Approximate Inverse** (AINV, SAINV, ...)

### Tasks for Preconditioned KSM



### Supplementary Accelerations (SA)

- ▶ Assign each task based on its characteristics.
  - CPU: good for serial algorithms, complex branches, frequent memory transfers.
  - GPU: good for massively data-parallel algorithms.
- ▶ Additional jobs run concurrently with main algorithms so that **accelerate the total throughput** as well as **convergence speed**.
- ▶ OpenCL fits well to the implementation of SA by estimating performances of each task and by scheduling the synchronization between heterogeneous resources.



## Implementation Issues

### OpenCL Scheduling

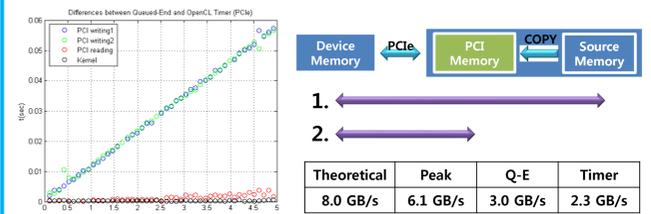
- ▶ In the CPU case, using full processing elements (PEs) will affect the performance because of scheduling overheads. Concurrency may not be guaranteed.



- ▶ `clCreateSubDevice()` creates sub-device as even or specific numbers of processing elements. Sub-division is considered to make one PE be managed for scheduler.

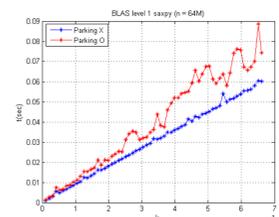
### PCI express Bandwidth

- ▶ Benchmarking PCI express performance shows big differences compared to SDK benchmark programs.
- ▶ Time measurements
  1. Overlapping by Linux timer between `clEnqueue*`.
  2. Profiling queue status from Queued to End.



### Windows Problems

- ▶ CPU parking protocol runs on Windows by default.
- ▶ This affects the performance in terms of context switching overheads.



### Integrated Processors Trials

- ▶ Integrated processors (Sandy- and Ivy-bridge, APU) share memory bandwidth for both the CPU and GPU.
- ▶ Simultaneous memory transfer will be serialized.

### Conclusion

- ▶ Heterogeneous computing with OpenCL tends to be very sensitive on its implementation.
- ▶ Relatively huge time has taken for configuring problems on concurrent executions.
- ▶ Task-parallel approach covers wider scopes of practical implementation, but it may be hard to split the target algorithm into sub-tasks.